

AP CALCULUS
U-SUBSTITUTION PRACTICE!

Name _____

1) $\int (x^3 - 1)^9 x^2 dx =$

- A) $\frac{(x^3 - 1)^8}{8} + c$
 B) $\frac{x^3(x^3 - 1)^{10}}{10} + c$
 C) $\frac{(x^3 - 1)^{10}}{10} + c$
 D) $\frac{x^3(x^3 - 1)^{10}}{30} + c$
 E) $\frac{(x^3 - 1)^{10}}{30} + c$

2) $\int x\sqrt{5x^2 - 3} dx =$

- A) $\frac{1}{15}(5x^2 - 3)^{\frac{3}{2}} + c$
 B) $\frac{x^2(5x^2 - 3)^{\frac{3}{2}}}{3} + c$
 C) $\frac{1}{10}(5x^2 - 3)^{\frac{3}{2}} + c$
 D) $\frac{2}{3}(5x^2 - 3)^{\frac{3}{2}} + c$
 E) $10(5x^2 - 3)^{\frac{3}{2}} + c$

3) $\int \frac{2x^2}{\sqrt{x^3 + 3}} dx =$

- A) $\frac{4}{3}\sqrt{x^3 + 3} + c$
 B) $\frac{2}{3}\sqrt{x^3 + 3} + c$
 C) $\frac{1}{3}\sqrt{x^3 + 3} + c$
 D) $\frac{4}{3\sqrt{x^3 + 3}} + c$
 E) $\frac{3}{4}\sqrt{x^3 + 3} + c$

4) $\int \frac{dx}{(5x + 3)^7} =$

- A) $\frac{1}{8(5x + 3)^8} + c$
 B) $-\frac{1}{30(5x + 3)^6} + c$
 C) $-\frac{1}{40(5x + 3)^8} + c$
 D) $-\frac{1}{6(5x + 3)^6} + c$
 E) $\frac{1}{30(5x + 3)^6} + c$

5) $\int \frac{(\sqrt{x} - 1)^5}{\sqrt{x}} dx =$

- A) $\frac{(\sqrt{x} - 1)^6}{12} + c$
 B) $\frac{(x\sqrt{x} - x)^6}{6} + c$
 C) $\frac{(x - \sqrt{x})^6}{6} + c$
 D) $\frac{(\sqrt{x} - 1)^6}{3} + c$
 E) $\frac{(\sqrt{x} - 1)^6}{6} + c$

6) $\int (x^2 + 1)(x^3 + 3x - 7)^{\frac{3}{5}} dx =$

- A) $\frac{5}{24}(x^3 + 3x - 7)^{\frac{8}{5}} + c$
 B) $\frac{5}{8}(x^3 + 3x - 7)^{\frac{8}{5}} + c$
 C) $\frac{1}{3}(x^3 + 3x - 7)^{\frac{2}{5}} + c$
 D) $\frac{5}{16}(x^2 + 1)^2(x^3 + 3x - 7)^{\frac{8}{5}} + c$
 E) $\frac{8}{15}(x^3 + 3x - 7)^{\frac{8}{5}} + c$

7) $\int \frac{dt}{\sqrt{t}(1-\sqrt{t})^2} =$

A) $-\frac{1}{2(1-\sqrt{t})^3} + c$

B) $-\frac{2}{3(1-\sqrt{t})^3} + c$

C) $\frac{2}{1-\sqrt{t}} + c$

D) $-\frac{2}{1-\sqrt{t}} + c$

E) $\frac{1}{2(1-\sqrt{t})} + c$

8) $\int \frac{x+2}{(x^2+4x-1)^2} dx =$

A) $-\frac{3}{(x^2+4x-1)^3} + c$

B) $\frac{x^2+2x}{6(x^2+4x-1)^3} + c$

C) $\frac{3}{(x^2+4x-1)^3} + c$

D) $-\frac{1}{2x^2+8x-2} + c$

E) $\frac{1}{2x^2+8x-2} + c$

9) $\int (x^2+2x+1)^{10} dx =$

A) $\frac{(x+1)^{19}}{19} + c$

B) $\frac{(x+1)^{21}}{21} + c$

C) $\frac{(x+1)^{13}}{13} + c$

D) $\frac{1}{11} \left(\frac{x^3}{3} + x^2 + x \right) 11 + c$

E) $\frac{(x^2+2x+1)^{11}}{11} + c$

10) If functions f and g are differentiable functions, then $\int g'(f(x)) f'(x) dx =$

- A) $g'(x) + c$
- B) $g(x) + c$
- C) $g(x) f(x) + c$
- D) $g(f'(x)) + c$
- E) $g(f(x)) + c$

11) $\int x\sqrt{x-1} dx =$

A) $\frac{2}{3}(x^2-x)^{\frac{3}{2}} + c$

B) $\frac{2}{5}(x-1)^{\frac{5}{2}} + \frac{2}{3}(x-1)^{\frac{3}{2}} + c$

C) $\frac{5}{2}(x-1)^{\frac{5}{2}} + \frac{3}{2}(x-1)^{\frac{3}{2}} + c$

D) $\frac{1}{3}x^2(x-1)^{\frac{3}{2}} + c$

E) $\frac{1}{2}(x-1)^4 + c$

12) $\int x^3 \cos x^4 dx =$

A) $\frac{x^4}{4} \sin x^4 + c$

B) $-\frac{1}{4} \sin x^4 + c$

C) $-\frac{x^4}{4} \sin x^4 + c$

D) $\frac{1}{4} \sin x^4 + c$

E) $\frac{x^4}{4} \sin \frac{x^5}{5} + c$

13) $\int \sin 5x dx =$

A) $\cos 5x + c$

B) $-5 \cos 5x + c$

C) $-\frac{1}{5} \cos 5x + c$

D) $\frac{1}{5} \cos 5x + c$

E) $5 \cos 5x + c$

14) $\int (\tan^3 x)(\sec^2 x) dx =$

A) $\frac{1}{4} \tan^4 x + c$

B) $\frac{1}{2} \sec^2 x + c$

C) $\frac{1}{2} \tan^2(x) + c$

D) $4 \tan^4 x + c$

E) $\frac{\sec^3 x \tan^4 x}{12} + c$

15) $\int \frac{\cos \sqrt{x}}{\sqrt{x}} dx =$

- A) $\frac{\cos^2 \sqrt{x}}{2x} + c$
 B) $2 \sin \sqrt{x} + c$
 C) $\frac{1}{2} \sin \sqrt{x} + c$
 D) $-\frac{1}{2} \sin \sqrt{x} + c$
 E) $-2 \sin \sqrt{x} + c$

16) $\int \sin 2\theta \cos 2\theta d\theta =$

- A) $\frac{1}{4} \sin^2 2\theta + c$
 B) $\frac{1}{2} \sin^2 2\theta + c$
 C) $-\frac{1}{4} \sin^2 2\theta + c$
 D) $-\frac{1}{2} \sin^2 2\theta + c$
 E) $\sin^2 2\theta + c$

17) $\int \frac{d\theta}{\cos^2 2\theta} =$

- A) $\frac{1}{2} \cot 2\theta + c$
 B) $\frac{1}{2} \tan 2\theta + c$
 C) $-\frac{2}{\cos 2\theta} + c$
 D) $2 \tan 2\theta + c$
 E) $-\frac{1}{2} \cot 2\theta + c$

18) $\int \sec^3 x \tan x dx =$

- A) $\frac{\tan^2 x}{2} + c$
 B) $\frac{\sec^2 x}{2} + c$
 C) $\frac{\sec^4 x \tan^2 x}{8} + c$
 D) $\frac{\sec^4 x}{4} + c$
 E) $\frac{\sec^3 x}{3} + c$

19) $\int \frac{\sin \frac{3}{\theta}}{\theta^2} d\theta =$

- A) $\frac{3 \cos^2 \left(\frac{3}{\theta}\right)}{\theta^3} + c$
 B) $-\frac{1}{3} \cos \frac{3}{\theta} + c$
 C) $\frac{\sin^2 \left(\frac{3}{\theta}\right)}{6\theta^3} + c$
 D) $-3 \cos \frac{3}{\theta} + c$
 E) $\frac{1}{3} \cos \frac{3}{\theta} + c$

20) $\int \cos(\cos x) \sin x dx =$

- A) $-\sin(\sin x) + c$
 B) $-\sin(\cos x) + c$
 C) $\cos(\cos x) + c$
 D) $\sin(\cos x) + c$
 E) $-\sin x + c$

21) $\int \frac{\cos 2\theta}{\sin^2 2\theta} d\theta =$

- A) $-\frac{1}{3 \sin^3 2\theta} + c$
 B) $-\frac{1}{6 \sin^3 2\theta} + c$
 C) $2 \sin 2\theta + c$
 D) $\frac{1}{2 \sin 2\theta} + c$
 E) $-\frac{1}{2 \sin 2\theta} + c$