

4. Show your work and circle the correct answer.

What are all values of  $x$  for which the series  $\sum_{n=1}^{\infty} \frac{(x-1)^n}{n}$  converges?

- ☒ A)  $-1 \leq x < 1$       ☐ C)  $0 < x < 2$       ☐ E)  $0 \leq x \leq 2$   
☐ B)  $-1 \leq x \leq 1$       ☒ D)  $0 \leq x < 2$

$$\lim_{n \rightarrow \infty} \frac{(x-1)^{n+1}}{n+1} \cdot \frac{n}{(x-1)^n} = (x-1)$$

~~all x~~

$$\frac{-1}{+1} < \frac{x-1}{+1} < \frac{1}{+1} \quad \text{Radius: } 1$$

$0 \leq x < 2$   
 $\downarrow$                        $\downarrow$   
 Converges          Diverges  
 AST                  P-series

5. Show your work and circle the correct answer.

The interval of convergence of  $\sum_{n=0}^{\infty} \frac{(x-1)^n}{3^n}$  is

- ☐ A)  $-3 < x \leq 3$       ☒ B)  $-2 < x < 4$       ☐ E)  $0 \leq x \leq 2$   
☐ C)  $-3 \leq x \leq 3$       ☐ D)  $-2 \leq x < 4$

$$\lim_{n \rightarrow \infty} \frac{(x-1)^{n+1}}{3^{n+1}} \cdot \frac{3^n}{(x-1)^n} = \frac{x-1}{3}$$

$$\frac{-1}{3} < \frac{x-1}{3} < \frac{1}{3}$$

$$\frac{-3}{+1} < \frac{x-1}{+1} < \frac{3}{+1} \quad \text{Radius: } 3$$

$$-2 < x < 4$$

$\downarrow$                        $\downarrow$   
 diverges          Diverges  
 Geometric      Geometric

6. Show your work and circle the correct answer.

What are all values of  $x$  for which the series  $\sum_{n=1}^{\infty} \frac{(x+2)^n}{\sqrt{n}}$  converges?

- ☐ A)  $-3 < x < -1$       ☒ B)  $-3 \leq x < -1$       ☐ C)  $-1 \leq x \leq 1$   
☒ D)  $-3 \leq x < -1$       ☐ E)  $-1 \leq x < 1$

$$\lim_{n \rightarrow \infty} \frac{(x+2)^{n+1}}{\sqrt{n+1}} \cdot \frac{\sqrt{n}}{(x+2)^n} = x+2$$

$$\frac{-1}{-2} < \frac{x+2}{-2} < \frac{1}{-2} \quad \text{Radius: } 1$$

$$-3 \leq x < -1$$

$\downarrow$                        $\downarrow$   
 Converges          Diverges  
 AST                  p-series

Answers are on the WEEBLY → UNIT 6 REVIEW