

Rolle's Theorem Practice

Verify that the hypotheses of Rolle's Theorem are satisfied on the given interval, and find all values of c in that interval that satisfy the conclusion of the theorem.

1. $f(x) = x^2 - 8x + 15$; $[3, 5]$

2. $f(x) = x^3 - 3x^2 + 2x$; $[0, 2]$

3. $f(x) = \cos x$; $\left[\frac{\pi}{2}, \frac{3\pi}{2}\right]$

4. $f(x) = \frac{1}{2}x - \sqrt{x}$; $[0, 4]$

5. $f(x) = \frac{1}{x^2} - \frac{4}{3x} + \frac{1}{3}$; $[1, 3]$

Mean Value Theorem

Verify that the hypotheses of the Mean-Value Theorem are satisfied on the given interval, and find all values of c in that interval that satisfy the conclusion of the theorem.

6. $f(x) = x^2 - x$; $[-3, 5]$

7. $f(x) = x^3 + x - 4$; $[-1, 2]$

8. $f(x) = \sqrt{x+1}$; $[0, 3]$

9. $f(x) = x - \frac{1}{x}$; $[3, 4]$

10. $f(x) = \sqrt{25 - x^2}$; $[-5, 3]$