SETS, SET NOTATION, AND OPERATIONS WITH SETS

SETS AND SET NOTATION

A set is a collection of objects called elements or members. The members of a set are either written using **roster notation**, which lists all the members of the set, or **set-builder notation**, which tells how the set is created. The elements of a set are displayed between brackets--{} and sets are named using capital letters.

For the multiples of five larger than 20,

Roster notation is {25, 30, 35, 40, 45, ...}. The three dots indicate to continue the pattern. Set-builder notation is $\{x | x > 20 \text{ and } x \text{ is a multiple of 5}\}$. This is read "the set of all x such that x is greater than 20 and a multiple of five."

Some very commonly used sets are:

 \mathbb{Z} --the set of integers

 \mathbb{Q} --the set of rational numbers, and

 \mathbb{N} --the set of natural numbers \mathbb{R} --the set of real numbers

Examples

Write in roster and set-builder notation.

M, the set of whole numbers less than ten.		B, the set of even, negative numbers.	
roster:	$M = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$	roster:	$B = \{\dots -8, -6, -4, -2\}$
set-builder:	M = { $x \mid x \text{ is whole and } x < 10$ }	set-builder:	$B = \{x x \text{ is even and } x < 0\}$

Problems

Write in roster and set-builder notation.

- 1. A, the set of integers greater than or equal to -5.
- 2. B. the integers divisible by three.
- 3. C, the integers between -2 and 2 inclusive.
- 4. D, the prime numbers less than 20.
- 5. E, the perfect squares between 10 and 100.
- 6. F, the odd integers less than 10.

UNION OF SETS

The **union** of two sets A and B, written $A \cup B$, is found by combining all of the elements that are in A, in B, or in both. When two mathematical equations or inequalities are joined by the word "*or*," it means to find the union of the two individual solutions.

Examples

Find the union of each pair of sets.

If A = {1, 3, 6, 10} and B = {3, 6, 9, 12, 15} then $A \cup B = \{1, 3, 6, 9, 10, 12, 15\}$

If $S = \{2, 4, 6, 8, 10\}$ and $T = \{4, 6, 10\}$ then $S \cup T = \{2, 4, 6, 8, 10\} = S$

Graph $\{x | x \ge -2\}$ or $\{x | x \ge 3\}$. The solution is the union of the two graphs.



Problems

Find the union of the two given sets.

- 7. $A = \{-3, -2, -1, 0, 1\}$ and $B = \{0, 1, 2, 3\}$
- 8. $C = \{0, 1, 2, 3, 4, 5\}$ and $D = \{0, 5, 10, 15\}$
- 9. $E = \{\dots -4, -2, 0, 2, 4, \dots\}$ and $F = \{\dots -3, -1, 1, 3, \dots\}$
- 10. $G = \{0, 2, 4, 6, 8, ...\}$ and $H = \{0, 4, 8, 12, ...\}$

Graph the solution.

- 11. $\{x | x \le 3\}$ or $\{x | x \le 5\}$
- 12. $\{x | x \ge 2\}$ or $\{x | \le -3\}$

13.
$$\{x | x \ge 2\}$$
 or $\{x | \le 3\}$

INTERSECTION OF SETS

The **intersection** of two sets A and B, written $A \cap B$, is found by listing all the elements that are common to both A and B. When two mathematical equations or inequalities are joined by the word "*and*," it means to find the intersection of the two individual solutions.

Examples

Find the intersection of each pair of sets.

- If A = {1, 3, 6, 10} and B = {3, 6, 9, 12, 15} then $A \cap B = {3, 6}$
- If $S = \{2, 4, 6, 8, 10\}$ and $T = \{4, 6, 10\}$ then $S \cap T = \{4, 6, 10\} = T$

Graph $\{x | x \ge -2\}$ and $\{x | x \le 3\}$. The solution is the intersection of the two graphs.



If two sets or two graphs have no common elements then their intersection is the empty set written $\{\}$ or \emptyset .

Problems

Find the intersection of the two given sets.

- 14. $A = \{0, 5, 10, 15, 20\}$ and $B = \{0, 10, 20, 30, 40\}$
- 15. $C = \{-3, -1, 0, 1, 3, 5, 7\}$ and $D = \{2, 3, 5, 7, 11, 13\}$
- 16. $E = \{0, 2, 4, 6, ...\}$ and $F = (0, 4, 8, 12, ...\}$
- 17. $G = \{1, 3, 5, 7, ...\}$ and $H = \{0, 10, 20, 30, ...\}$

Graph the solution.

- 18. $\{x | x \ge 2\}$ and $\{x | \le 5\}$
- 19. $\{x | x \le -2\}$ and $\{x | \le 5\}$
- 20. $\{x | x \le -2\}$ and $\{x | \ge 2\}$

Answers

1. $A = \{ -5, -4, -3, -2, -1, 0, \}$	2. $B = \{, -6, -3, 0, 3,\}$
$A = \left\{ x x \text{ is integer and } x \ge -5 \right\}$	$\mathbf{B} = \left\{ x \mid x \text{ is divisible by 3} \right\}$
3. $C = \{-2, -1, 0, 1, 2\}$	4. $D = \{2, 3, 5, 7, 11, 13, 17\}$
$C = \left\{ x x \text{ is integer and } -2 \le x \le 2 \right\}$	$D = \left\{ x x \text{ is prime and } x < 20 \right\}$
5. $E = \{16, 25, 36, 49, 64, 81\}$	6. $F = \{, -1, 1, 3, 5, 7, 9\}$
$\mathbf{E} = \left\{ x \mid x \text{ is square and } 10 < x < 100 \right\}$	$\mathbf{F} = \left\{ x \mid x \text{ is odd integer and } x < 10 \right\}$
7. $\{-3, -2, -1, 0, 1, 2, 3\}$	8. {0, 1, 2, 3, 4, 5, 10, 15}
9. {,-2, -1, 0, 1, 2,} or Z	10. $\{0, 2, 4, 6, \ldots\}$
11.	12.
$\overset{\leftarrow}{} \overset{\leftarrow}{} $	-3 0 2
13. all real numbers	14. {0, 10, 20}
15. {3, 5, 7}	16. $\{0, 4, 8, 12, \ldots\}$
17. Ø	18. ••••••••••••••••••••••••••••••••••••
19. -2 0	20. Ø