# Sample Problems

Compute each of the following integrals. Please note that  $\arcsin x$  is the same as  $\sin^{-1} x$  and  $\arctan x$  is the same as  $\tan^{-1} x$ 

1. 
$$\int xe^{x} dx$$
  
2. 
$$\int x \cos x dx$$
  
3. 
$$\int xe^{-4x} dx$$
  
4. 
$$\int \ln x dx$$
  
5. 
$$\int \arcsin x dx$$
  
6. 
$$\int \arctan x dx$$
  
7. 
$$\int e^{x} \sin x dx$$
  
8. 
$$\int \sin^{2} x dx$$
  
9. 
$$\int \cos^{2} x dx$$
  
10. 
$$\int x^{2}e^{-3x} dx$$
  
11. 
$$\int \frac{x^{3}}{(x^{2}+2)^{2}} dx$$

# Practice Problems

1. 
$$\int xe^{2x} dx$$
  
2. 
$$\int xe^{-3x} dx$$
  
3. 
$$\int_{0}^{\ln 2} xe^{-3x} dx$$
  
4. 
$$\int_{0}^{\infty} xe^{-3x} dx$$
  
5. 
$$\int x2^{x} dx$$
  
6. 
$$\int x^{2}2^{x} dx$$
  
7. 
$$\int x\cos x dx$$
  
8. 
$$\int x\cos x dx$$
  
9. 
$$\int x\ln x dx$$
  
10. 
$$\int x^{5}\ln x dx$$
  
11. 
$$\int x\sin 10x dx$$
  
12. 
$$\int_{1}^{9} \frac{\ln x}{\sqrt{x}} dx$$
  
13. 
$$\int_{1}^{\infty} \frac{\ln x}{x^{7}} dx$$
  
14. 
$$\int_{0}^{\pi/4} x\sin 2x dx$$

# Sample Problems - Answers

1.) 
$$xe^{x} - e^{x} + C$$
 2.)  $x\sin x + \cos x + C$  3.)  $-\frac{1}{16}e^{-4x} - \frac{1}{4}xe^{-4x} + C$  4.)  $x\ln x - x + C$   
5.)  $x\arcsin x + \sqrt{1 - x^{2}} + C$  6.)  $x\arctan x - \frac{1}{2}\ln(x^{2} + 1) + C$  7.)  $\frac{1}{2}e^{x}(\sin x - \cos x) + C$   
8.)  $\frac{1}{2}(-\sin x\cos x + x) + C$  9.)  $\frac{1}{2}(x + \sin x\cos x) + C$  10.)  $-e^{-3x}\left(\frac{1}{3}x^{2} + \frac{2}{9}x + \frac{2}{27}\right)$   
11.)  $\frac{1}{2}\ln(x^{2} + 2) + \frac{1}{x^{2} + 2} + C$ 

## Practice Problems - Answers

1.) 
$$\frac{1}{2}xe^{2x} - \frac{1}{4}e^{2x} + C$$
  
2.)  $-\frac{1}{9}e^{-3x} - \frac{1}{3}xe^{-3x} + C$   
3.)  $\frac{7}{72} - \frac{1}{24}\ln 2$   
4.)  $\frac{1}{9}$   
5.)  $\frac{2^{x}}{\ln 2}\left(x - \frac{1}{\ln 2}\right) + C$   
6.)  $\frac{2^{x}}{\ln 2}\left(x^{2} - \frac{2x}{\ln 2} + \frac{2}{\ln^{2}2}\right) + C$   
7.)  $x\sin x + \cos x + C$   
8.)  $x^{2}\sin x + 2x\cos x - 2\sin x + C$   
9.)  $\frac{1}{2}x^{2}\ln x - \frac{1}{4}x^{2} + C$   
10.)  $\frac{1}{6}x^{6}\ln x - \frac{1}{36}x^{6} + C$ 

11.) 
$$\frac{1}{100}\sin 10x - \frac{1}{10}x\cos 10x + C$$
 12.)  $6\ln 9 - 8$  13.)  $\frac{1}{36}$  14)  $\frac{1}{4}$ 

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### Sample Problems - Solutions

Please note that  $\arcsin x$  is the same as  $\sin^{-1} x$  and  $\arctan x$  is the same as  $\tan^{-1} x$ .

1. 
$$\int xe^x dx$$

Solution: We will integrate this by parts, using the formula

$$\int f'g = fg - \int fg'$$

Let g(x) = x and  $f'(x) = e^x$  Then we obtain g' and f by differentiation and integration.

$f\left(x\right) = e^{x}$	$g\left(x\right) = x$
$f'(x) = e^x$	$g'\left(x\right) = 1$

$$\int f'g = fg - \int fg' \text{ becomes}$$

$$\int xe^x dx = xe^x - \int e^x dx = \boxed{xe^x - e^x + C}$$

We should check our result by differentiating the answer. Indeed,

$$(xe^{x} - e^{x} + C)' = e^{x} + xe^{x} - e^{x} = xe^{x}$$

and so our answer is correct.

2.  $\int x \cos x \, dx$ 

Solution: Let g(x) = x and  $f'(x) = \cos x$  Then we obtain g' and f by differentiation and integration.

$$\begin{aligned} f(x) &= \sin x \quad g(x) = x \\ f'(x) &= \cos x \quad g'(x) = 1 \end{aligned}$$
$$\int f'g &= fg - \int fg' \quad \text{becomes} \\ \int x \cos x \, dx &= x \sin x - \int \sin x \, dx = x \sin x - (-\cos x) = \boxed{x \sin x + \cos x + C} \end{aligned}$$

We should check our result by differentiating the answer. Indeed,

 $(x\sin x + \cos x + C)' = \sin x + x\cos x - \sin x = x\cos x$ 

and so our answer is correct.

3. 
$$\int x e^{-4x} dx$$

Solution: Let g(x) = x and  $f'(x) = e^{-4x}$  Then we obtain g' and f by differentiation and integration. To compute f(x), we will use substitution. Let u = -4x then du = -4dx and so  $dx = \frac{du}{-4}$ .

$$f(x) = \int e^{-4x} dx = \int e^u \frac{du}{-4} = -\frac{1}{4} \int e^u du = -\frac{1}{4} e^u + C = -\frac{1}{4} e^{-4x} + C$$

We will choose C = 0 and so  $f(x) = -\frac{1}{4}e^{-4x}$ .

$$\begin{aligned} f(x) &= -\frac{1}{4}e^{-4x} \quad g(x) = x\\ \hline f'(x) &= e^{-4x} \quad g'(x) = 1 \end{aligned}$$

$$\int f'g \quad = \quad fg - \int fg' \quad \text{becomes}\\ \int xe^{-4x} \, dx \quad = \quad -\frac{1}{4}xe^{-4x} - \int -\frac{1}{4}e^{-4x} \, dx = -\frac{1}{4}xe^{-4x} + \frac{1}{4}\int e^{-4x} \, dx = -\frac{1}{4}xe^{-4x} + \frac{1}{4}\left(-\frac{1}{4}e^{-4x}\right) + C\\ &= \quad \left[-\frac{1}{4}xe^{-4x} - \frac{1}{16}e^{-4x} + C\right]\end{aligned}$$

We check our result by differentiating the answer.

$$\left(-\frac{1}{4}xe^{-4x} - \frac{1}{16}e^{-4x} + C\right)' =$$

$$= -\frac{1}{4}\left(xe^{-4x}\right)' - \frac{1}{16}\left(e^{-4x}\right)' = -\frac{1}{4}\left(e^{-4x} + x\left(-4e^{-4x}\right)\right) - \frac{1}{16}\left(-4e^{-4x}\right)$$

$$= -\frac{1}{4}e^{-4x} + xe^{-4x} + \frac{1}{4}e^{-4x} = xe^{-4x}$$

and so our answer is correct.

4. 
$$\int \ln x \, dx$$

Solution: Let  $g(x) = \ln x$  and f'(x) = 1 Then we obtain g' and f by differentiation and integration.  $\begin{array}{c|c}
f(x) = x & g(x) = \ln x \\
\hline
f'(x) = 1 & g'(x) = \frac{1}{x}
\end{array}$ 

$$\int f'g = fg - \int fg' \text{ becomes}$$

$$\int \ln x \, dx = x \ln x - \int x \cdot \frac{1}{x} \, dx = x \ln x - \int 1 \, dx = \boxed{x \ln x - x + C}$$

We check our result by differentiating the answer.

$$(x \ln x - x + C)' = \ln x + x \cdot \frac{1}{x} - 1 = \ln x$$

and so our answer is correct.

# 5. $\int \arcsin x \, dx$

Solution: Let  $g(x) = \arcsin x$  and f'(x) = 1 Then we obtain g' and f by differentiation and integration.

$$\begin{aligned} f(x) &= x \quad g(x) = \arcsin x \\ f'(x) &= 1 \quad g'(x) = \frac{1}{\sqrt{1 - x^2}} \end{aligned}$$

$$\int f'g &= fg - \int fg' \quad \text{becomes} \\ \int \arcsin x \, dx &= x \arcsin x - \int x \cdot \frac{1}{\sqrt{1 - x^2}} \, dx = x \arcsin x - \int \frac{x}{\sqrt{1 - x^2}} \, dx \end{aligned}$$

We compute the integral  $\int \frac{x}{\sqrt{1-x^2}} dx$  by substitution. Let  $u = 1 - x^2$ . Then du = -2xdx and so  $dx = \frac{du}{-2x}$ .

$$\int \frac{x}{\sqrt{1-x^2}} \, dx = \int \frac{x}{\sqrt{u}} \frac{du}{-2x} = -\frac{1}{2} \int \frac{1}{\sqrt{u}} \, du = -\frac{1}{2} \int u^{-1/2} \, du$$
$$= -\frac{1}{2} \frac{u^{1/2}}{\frac{1}{2}} + C = -\sqrt{u} + C = -\sqrt{1-x^2} + C$$

Thus the entire integral is

$$\int \arcsin x \, dx = x \arcsin x - \left(-\sqrt{1-x^2}\right) + C = \boxed{x \arcsin x + \sqrt{1-x^2} + C}$$

We check our result by differentiating the answer.

$$\left(x \arcsin x + \sqrt{1 - x^2} + C\right)' =$$

$$= (x \arcsin x)' + \left(\left(1 - x^2\right)^{1/2}\right)' = \arcsin x + x \cdot \frac{1}{\sqrt{1 - x^2}} + \frac{1}{2}\left(1 - x^2\right)^{-1/2} (-2x)$$

$$= \arcsin x + \frac{x}{\sqrt{1 - x^2}} - \frac{x}{\sqrt{1 - x^2}} = \arcsin x$$

and so our answer is correct.

6. 
$$\int \arctan x \, dx$$

Solution: Let  $g(x) = \arctan x$  and f'(x) = 1 Then we obtain g' and f by differentiation and integration.

### Last revised: December 10, 2013

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We compute the integral  $\int \frac{x}{x^2+1} dx$  by substitution. Let  $u = x^2+1$ . Then du = 2xdx and so  $dx = \frac{du}{2x}$ .

$$\int \frac{x}{x^2 + 1} \, dx = \int \frac{x}{u} \, \frac{du}{2x} = \frac{1}{2} \int \frac{1}{u} \, du = \frac{1}{2} \ln |u| + C = \frac{1}{2} \ln \left(x^2 + 1\right) + C$$

Thus the entire integral is

$$\int \arctan x \, dx = \boxed{x \arctan x - \frac{1}{2} \ln \left(x^2 + 1\right) + C}$$

We check our result by differentiating the answer.

$$\left(x \arctan x - \frac{1}{2}\ln\left(x^{2} + 1\right) + C\right)' =$$

$$= (x \arctan x)' - \frac{1}{2}\left(\ln\left(x^{2} + 1\right)\right)' = \arctan x + x \cdot \frac{1}{x^{2} + 1} - \frac{1}{2}\frac{1}{x^{2} + 1}\left(2x\right)$$

$$= \arctan x + \frac{x}{x^{2} + 1} - \frac{x}{x^{2} + 1} = \arctan x$$

so our answer is correct.

7.  $\int e^x \sin x \, dx$ 

Solution: This is an interesting application of integration by parts. Let M denote the integral  $\int e^x \sin x \, dx$ . Solution: Let  $g(x) = \sin x$  and  $f'(x) = e^x$  (Notice that because of the symmetry,  $g(x) = e^x$  and  $f'(x) = \sin x$  would also work.) We obtain g' and f by differentiation and integration.

$f\left(x\right) = e^x$	$g\left(x\right) = \sin x$
$f'\left(x\right) = e^x$	$g'\left(x\right) = \cos x$

$$\int f'g = fg - \int fg' \text{ becomes}$$

$$\int e^x \sin x \, dx = e^x \sin x - \int e^x \cos x \, dx$$

It looks like our method produced a new integral,  $\int e^x \cos x \, dx$  that also requires integration by parts. We proceed: let  $g(x) = \cos x$  and  $f'(x) = e^x$ . We obtain g' and f by differentiation and integration.

$$\begin{aligned} f(x) &= e^x \quad g(x) = \cos x \\ f'(x) &= e^x \quad g'(x) = -\sin x \end{aligned}$$

$$\int f'g &= fg - \int fg' \quad \text{becomes} \\ \int e^x \cos x \, dx &= e^x \cos x - \int e^x (-\sin x) \, dx = e^x \cos x + \int e^x \sin x \, dx \end{aligned}$$

$$Thus \int e^x \cos x \, dx = e^x \cos x + \int e^x \sin x \, dx$$

Now the result contains the original integral,  $\int e^x \sin x$ . At this point, it looks like we are getting nowhere because we are going in circles. However, this is not the case. Recall that we denote  $\int e^x \sin x$  by M. Let us review the computation again:

$$\int e^x \sin x \, dx = e^x \sin x - \int e^x \cos x \, dx$$
$$\int e^x \sin x \, dx = e^x \sin x - \left(e^x \cos x + \int e^x \sin x \, dx\right)$$
$$\int e^x \sin x \, dx = e^x \sin x - e^x \cos x - \int e^x \sin x \, dx$$

This is the same as

 $M = e^x \sin x - e^x \cos x - M$ 

This is an equation that we can solve for M.

$$2M = e^x \sin x - e^x \cos x$$
$$M = \frac{1}{2}e^x (\sin x - \cos x)$$

Thus the answer is  $\boxed{\frac{1}{2}e^x(\sin x - \cos x) + C}$ . We check our result by differentiation.

$$\left(\frac{1}{2}e^{x}\left(\sin x - \cos x\right)\right) = \frac{1}{2}\left(e^{x}\right)'\left(\sin x - \cos x\right) + \frac{1}{2}e^{x}\left(\sin x - \cos x\right)' = \frac{1}{2}e^{x}\left(\sin x - \cos x\right) + \frac{1}{2}e^{x}\left(\cos x + \sin x\right) = \frac{1}{2}e^{x}\left(\sin x - \cos x + \sin x + \cos x\right) = \frac{1}{2}e^{x}\left(2\sin x\right) = e^{x}\sin x$$

so our answer is correct.

8.  $\int \sin^2 x \, dx$ 

Solution: Note that this integral can be easily solved using substitution. This is because of the double angle formula for cosine,  $\cos 2x = 1 - 2\sin^2 x \implies \sin^2 x = \frac{1 - \cos 2x}{2}$ . This solution can be found on our substitution handout. But at the moment, we will use this interesting application of integration by parts as seen in the previous problem.

Let *M* denote the integral  $\int \sin^2 x \, dx$ . Let  $g(x) = \sin x$  and  $f'(x) = \sin x$  Then we obtain g' and f by differentiation and integration.

$$\frac{f(x) = -\cos x}{f'(x) = \sin x} \quad g(x) = \sin x$$

$$\int f'g = fg - \int fg' \quad \text{becomes}$$

$$\int \sin^2 x \, dx = -\sin x \cos x - \int (-\cos x) \cos x \, dx = -\sin x \cos x + \int \cos^2 x \, dx$$

$$= -\sin x \cos x + \int 1 - \sin^2 x \, dx = -\sin x \cos x + \int 1 \, dx - \int \sin^2 x \, dx$$

$$= -\sin x \cos x + x - \int \sin^2 x \, dx$$

We obtained

$$\int \sin^2 x \, dx = -\sin x \cos x + x - \int \sin^2 x \, dx \quad \text{or}$$

$$M = -\sin x \cos x + x - M \quad \text{we solve for } M$$

$$2M = -\sin x \cos x + x$$

$$M = \frac{1}{2} \left( -\sin x \cos x + x \right) + C$$

$$(-\sin x \cos x + x) + C$$
We check our result by differentiating the formula of the constant of the cons

So our answer is  $\boxed{\frac{1}{2}}$ the answer.

$$\left(\frac{1}{2}\left(-\sin x\cos x + x\right) + C\right)' =$$

$$= \left(\frac{1}{2}\left(-\sin x \cos x + x\right) + C\right)' = \frac{1}{2}\left(-\sin x \left(-\sin x\right) + \left(-\cos x\right) \left(\cos x\right) + 1\right)$$
$$= \frac{1}{2}\left(\sin^2 x - \cos^2 x + 1\right) = \frac{1}{2}\left(\sin^2 x + \underbrace{1 - \cos^2 x}_{\sin^2 x}\right) = \frac{1}{2}\left(2\sin^2 x\right) = \sin^2 x$$

so our answer is correct.

9.  $\int \cos^2 x \ dx$ 

Solution: We do not need to integrate by parts (although it is good practice)

$$\int \cos^2 x \, dx = \int 1 - \sin^2 x \, dx = \int 1 \, dx - \int \sin^2 x \, dx = x - \frac{1}{2} \left( -\sin x \cos x + x \right) + C$$
$$= \frac{1}{2} \sin x \cos x + \frac{1}{2} x + C = \boxed{\frac{1}{2} \left( x + \sin x \cos x \right) + C}$$

We check our result by differentiating the answer.

$$\left(\frac{1}{2}\left(x+\sin x\cos x\right)+C\right)' = \frac{1}{2}\left(1+\cos^2 x-\sin^2 x\right) = \frac{1}{2}\left(\underbrace{1-\sin^2 x}_{\cos^2 x}+\cos^2 x\right) = \frac{1}{2}\left(2\cos^2 x\right) = \cos^2 x$$

so our answer is correct.

10. 
$$\int x^2 e^{-3x} dx$$

Solution: We will need to integrate by parts twice. First, let  $f'(x) = e^{-3x}$  and  $g(x) = x^2$ . Then  $\begin{array}{rcl}
\hline f(x) = -\frac{1}{3}e^{-3x} & g(x) = x^2 \\
\hline f'(x) = e^{-3x} & g'(x) = 2x
\end{array}$   $\int f'g &= fg - \int fg' \quad \text{becomes} \\
\int x^2 e^{-3x} dx &= -\frac{1}{3}e^{-3x} \left(x^2\right) - \int \left(-\frac{1}{3}e^{-3x}\right) 2x dx = -\frac{1}{3}x^2 e^{-3x} + \frac{2}{3}\int x e^{-3x} dx$ 

and we can compute  $\int xe^{-3x} dx$  by integrating by parts. Let  $f'(x) = e^{-3x}$  and g(x) = x. Then

$$\frac{f(x) = -\frac{1}{3}e^{-3x}}{f'(x) = e^{-3x}} \frac{g(x) = x}{g'(x) = 1}$$

$$\int f'g = fg - \int fg' \text{ becomes}$$

$$\int xe^{-3x} dx = -\frac{1}{3}e^{-3x}(x) - \int \left(-\frac{1}{3}e^{-3x}\right) dx = -\frac{1}{3}xe^{-3x} + \frac{1}{3}\int e^{-3x} dx$$

$$= -\frac{1}{3}xe^{-3x} + \frac{1}{3}\left(-\frac{1}{3}e^{-3x}\right) + C = -\frac{1}{3}xe^{-3x} - \frac{1}{9}e^{-3x} + C$$

This is the result we need to compute the integral  $\int x^2 e^{-3x} dx$ . So far we had this much:

$$\int x^2 e^{-3x} \, dx = -\frac{1}{3}x^2 e^{-3x} + \frac{2}{3} \int x e^{-3x} \, dx$$

to this we substitute our result  $\int xe^{-3x} dx = -\frac{1}{3}xe^{-3x} - \frac{1}{9}e^{-3x} + C$ :

$$\int x^2 e^{-3x} dx = -\frac{1}{3}x^2 e^{-3x} + \frac{2}{3}\int x e^{-3x} dx = -\frac{1}{3}x^2 e^{-3x} + \frac{2}{3}\left(-\frac{1}{3}x e^{-3x} - \frac{1}{9}e^{-3x} + C_1\right)$$
$$= -\frac{1}{3}x^2 e^{-3x} - \frac{2}{9}x e^{-3x} - \frac{2}{27}e^{-3x} + C$$

Our result might look nicer if we factor out  $-e^{-3x}$  or  $-\frac{1}{27}e^{-3x}$ . Then the final answer is  $\boxed{-e^{-3x}\left(\frac{1}{3}x^2+\frac{2}{9}x+\frac{2}{27}\right)+C} \text{ or } \boxed{-\frac{1}{27}e^{-3x}\left(9x^2+6x+2\right)+C}.$ 

We check via differentiation:

$$f'(x) = \left(-\frac{1}{27}e^{-3x}\left(9x^2+6x+2\right)\right)' = -\frac{1}{27}\left(-3e^{-3x}\left(9x^2+6x+2\right)+e^{-3x}\left(18x+6\right)\right)$$
$$= -\frac{1}{27}\left(e^{-3x}\left(-27x^2-18x-6\right)+e^{-3x}\left(18x+6\right)\right)$$
$$= -\frac{1}{27}e^{-3x}\left(-27x^2-18x-6+18x+6\right) = x^2e^{-3x}$$

and so our solution is correct.

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11. 
$$\int \frac{x^3}{(x^2+2)^2} dx$$

Solution: this integral can be computed using at least three different methods: substitution (try  $u = x^2 + 2$ ) or partial fractions or integration by parts. We will present integration by parts here.

First, let  $f'(x) = \frac{x}{(x^2+2)^2}$  and  $g(x) = x^2$ . To compute f, we need to integrate  $\frac{x}{(x^2+2)^2}$ . We can do

that by using substitution: Let  $u = x^2 + 2$ . Then du = 2xdx and so  $dx = \frac{du}{2x}$ . So

$$\int \frac{x}{\left(x^2+2\right)^2} \, dx = \int \frac{x}{u^2} \, \frac{du}{2x} = \frac{1}{2} \int \frac{1}{u^2} \, du = \frac{1}{2} \left(-\frac{1}{u}\right) + C = -\frac{1}{2\left(x^2+2\right)} + C$$

Thus if  $f'(x) = \frac{x}{(x^2+2)^2}$ , then  $f(x) = -\frac{1}{2(x^2+2)}$ . Proceeding with the integration by parts, we write

$$\begin{array}{c}
f(x) = -\frac{1}{2(x^2 + 2)} & g(x) = x^2 \\
f'(x) = \frac{x}{(x^2 + 2)^2} & g'(x) = 2x
\end{array}$$

$$\int f'g = fg - \int fg' \text{ becomes}$$

$$\int \frac{x}{(x^2+2)^2} (x^2) dx = -\frac{1}{2(x^2+2)} (x^2) - \int -\frac{1}{2(x^2+2)} (2x) dx$$

$$= -\frac{x^2}{2(x^2+2)} + \int \frac{x}{x^2+2} dx$$

and this second integral can be computed using the same substitution:

Let  $w = x^2 + 2$ . Then dw = 2xdx and so  $dx = \frac{dw}{2x}$  $\int \frac{x}{x^2 + 2} dx = \int \frac{x}{w} \frac{dw}{2dx} = \frac{1}{2} \int \frac{1}{w} dw = \frac{1}{2} \ln|w| + C = \frac{1}{2} \ln(x^2 + 2) + C$ 

and so the entire integral is then

$$\int \frac{x^3}{\left(x^2+2\right)^2} \, dx = -\frac{x^2}{2\left(x^2+2\right)} + \int \frac{x}{x^2+2} \, dx = \boxed{-\frac{x^2}{2\left(x^2+2\right)} + \frac{1}{2}\ln\left(x^2+2\right) + C}$$

We check via differentiation:

$$f'(x) = \left(-\frac{x^2}{2(x^2+2)} + \frac{1}{2}\ln(x^2+2) + C\right)'$$
  
=  $-\frac{1}{2}\left(\frac{2x(x^2+2) - x^2(2x)}{(x^2+2)^2}\right) + \frac{1}{2}\frac{1}{x^2+2}(2x)$   
=  $-\left(\frac{x(x^2+2) - x^3}{(x^2+2)^2}\right) + \frac{x}{x^2+2} = -\left(\frac{x^3+2x-x^3}{(x^2+2)^2}\right) + \frac{x}{x^2+2}$   
=  $-\frac{2x}{(x^2+2)^2} + \frac{x(x^2+2)}{(x^2+2)^2} = \frac{-2x+x^3+2x}{(x^2+2)^2} = \frac{x^3}{(x^2+2)^2}$ 

and so our solution is correct.

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